

Syllabus of Math 5181

- (1) neighborhoods, bases, and subbases, closure operator
- (2) countability, linear orders and topology, well-ordering
- (3) subspaces, products, continuous functions, weak topologies
- (4) sequences, nets, and filters
- (5) separation axioms and preservation properties
- (6) completely regular, normal spaces, Urysohn's lemma
- (7) countability properties, Urysohn's metrization theorem, Tietze extension theorem
- (8) standard examples like irrationals, Sorgenfrey line and plane, lexicographic square, Tychonoff plank, Alexandroff double, double arrow.
- (9) compact spaces, locally compact spaces, compactifications
- (10) products of compact, countably compact, normal spaces,
- (11) metrization, complete metric spaces, the Baire Theorem,
- (12) connectedness, local connectedness, continua, path-connected, components
- (13) Cantor set, totally disconnected spaces
- (14) Tychonoff's theorem.